Model Question Paper-I with effect from 2022 (CBCS Scheme)

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Second Semester B.E Degree Examination
Mathematics-II for Computer Science Engineering-BMATS201

TIME: 03 Hours   Max. Marks: 100

Note:
1. Answer any **FIVE** full questions, choosing at least **ONE** question from each **module**.
2. VTU Formula Hand Book is permitted.
3. M: Marks, L: Bloom's level, C: Course outcomes.

		Module -1	M	L	C
Q.01	a	Evaluate $\int_0^a \int_0^x \int_0^{x+y} e^{x+y+z}\, dz\, dy\, dx$	7	L2	CO1
	b	Evaluate $\int_0^\infty \int_0^\infty e^{-(x^2+y^2)}\, dx\, dy$ by changing into polar coordinates.	7	L2	CO1
	c	Show that $\beta(m,n) = \frac{\gamma(m)\gamma(n)}{\gamma(m+n)}$	6	L2	CO1
		OR			
Q.02	a	Evaluate $\int_0^a \int_y^a \frac{x}{x^2+y^2} dxdy$ by changing the order of integration	7	L2	CO1
	b	Using double integration find the area of a plate in the form of a quadrant of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$	7	L3	CO1
	c	Write the codes to find the volume of the tetrahedron bounded by the planes $x=0,\ y=0\ and\ z=0, \frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ using Mathematical tools.	6	L3	CO5
		Module-2			
Q. 03	a	Find $\nabla\phi$, if $\phi = x^3 + y^3 + z^3 - 3xyz$ at the point $(1,-1,2)$	7	L2	CO2
	b	If $\vec{F} = \nabla(x^3 + y^3 + z^3 - 3xyz)$ find $div\ \vec{F}$ and $curl\ \vec{F}$	7	L2	CO2
	c	Express the vector $\vec{A} = z\hat{\imath} - 2x\hat{\jmath} + y\hat{k}$ in cylindrical coordinates.	6	L2	CO2
		OR			
Q.04	a	Find the directional derivative of $\phi = x^2\, yz + 4xz^2$ at $(1, -2, -1)$ in the direction of the vector $2\hat{\imath} - \hat{\jmath} - 2\hat{k}$.	7	L2	CO2
	b	Show that the spherical coordinate system is orthogonal	7	L3	CO2
	c	Using the Mathematical tools, write the codes to find the gradient of	6	L3	CO5

		$\emptyset = x^2 yz.$			
Module-3					
Q. 05	a	Prove that the subset W = {(x, y, z) | x – 3y + 4z = 0} of the vector space R³ is a subspace of R³.	**7**	L3	**CO3**
	b	Determine whether the matrix $\begin{bmatrix} -1 & 7 \\ 8 & -1 \end{bmatrix}$ is a linear combination of $\begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}, \begin{bmatrix} 2 & -3 \\ 0 & 2 \end{bmatrix}$ and $\begin{bmatrix} 0 & 1 \\ 2 & 0 \end{bmatrix}$ in the vector space M₂₂ of 2 ×2 matrices.	**7**	L2	**CO3**
	c	Find the matrix of the linear transformation T: V₂(R) → V₃(R) such that T (−1, 1) = (−1, 0, 2) and T (2, 1) = (1, 2, 1).	**6**	L2	**CO3**
OR					
Q. 06	a	Show that the set S = {(1, 2, 4), (1, 0, 0), (0, 1, 0), (0, 0, 1)} is linearly dependent.	**7**	L2	**CO3**
	b	Let Pₙ be the vector space of real polynomial functions of degree ≤ n. Show that the transformation $T: P_2 \rightarrow P_1$ defined by $T (ax^2 + bx + c) = (a + b) x + c$ is linear.	**7**	L2	**CO3**
	c	Verify the Rank-nullity theorem for the linear transformation T: V₃(R) → V₂(R) defined by $T (x, y, z) = (y - x, y - z).$	**6**	L2	**CO3**
Module-4					
Q. 07	a	Find the real root of the equation $3x = \cos x + 1$ correct to three decimal places using Newton's Raphson method.	**7**	L2	**CO4**
	b	Find y at $x = 5$ if $y(1) = -3,\ y(3) = 9, y(4) = 30, y(6) = 132$ using Lagrange's interpolation formula.	**7**	L2	**CO4**
	c	Evaluate $\int_0^1 \frac{1}{1+x} dx$ by taking 7 ordinates and by using Simpson's 3/8 rule.	**6**	L3	**CO4**
OR					
Q. 08	a	Find an approximate root of the equation $x^3 - 3x + 4 = 0$ using the method of false position, correct to three decimal places which lie between -3 and -2. (Carry out three iterations).	**7**	L2	**C04**

	b	Using Newton's appropriate interpolation formula, find the values of y at $x = 8$ and at $x = 22$ from the following table:	7	L3	CO4

x	0	5	10	15	20	25
y	7	11	14	18	24	32

	c	Evaluate $\int_0^{\frac{\pi}{2}} \sqrt{\cos x}\, dx$ by using the Trapezoidal rule by taking 7 ordinates.	6	L2	CO4

Module-5

Q. 09	a	Solve $y'(x) = 3x + \frac{y}{2}$, $y(0) = 1$ then find $y(0.2)$ with $h = 0.2$ using modified Euler's method.	7	L2	CO4
	b	Apply Runge-Kutta method of fourth order to find an approximate value of y when x = 0.2 given that $\frac{dy}{dx} = x + y$ and y = 1 when x = 0.	7	L2	CO4
	c	Given $\frac{dy}{dx} = xy + y^2$, $y(0) = 1, y(0.1) = 1.1169$, $y(0.2) = 1.2773$, $y(0.3) = 1.5049$ compute $y(0.4)$ using Milne's method.	6	L2	CO4

OR

Q. 10	a	Employ Taylor's series method to obtain approx. value of y at x = 0.2 for the differential equation $\frac{dy}{dx} = 2y + 3e^x, y(0) = 0$.	7	L2	CO4
	b	Using the Runge-Kutta method of fourth order, solve $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ with $y(0) = 1$ at x = 0.2.	7	L2	CO4
	c	Write the Mathematical tool codes to solve the differential equation $\frac{dy}{dx} - 2y = 3e^x$ with y(0) = 0 using the Taylors series method at x = 0.1(0.1)0.3.	6	L3	CO5